

Prove this identity:

$$\frac{\csc(x)-1}{\csc(x)+1} = \frac{1-\sin(x)}{1+\sin(x)}$$

Ans:

LHS

$$\begin{aligned} & \frac{\frac{1}{\sin(x)} - 1}{\frac{1}{\sin(x)} + 1} \end{aligned}$$

Multiply top and bottom by $\sin(x)$

$$= \frac{\frac{1}{\sin(x)} - 1}{\frac{1}{\sin(x)} + 1} * \frac{\sin(x)}{\sin(x)}$$

$$= \frac{1-\sin(x)}{1+\sin(x)}$$