(8 points)
5. A study included 200 men and 280 women to see whether people differ by gender in their sensitivity to smells. Use the data to test to claim that the proportion of sensitive women is greater than the proportion of sensitive men. Do not analyze this as a contingency table. (Use $\alpha=0.05$ for this test.)

| Gender | Men | Women |
| ---: | ---: | ---: |
| Sensitive | 20 | 42 |
| Insensitive | 180 | 238 |
| Total | 200 | 280 |

(8 points)
5. A study included 200 men and 280 women to see whether people differ by gender in their sensitivity to smells. Use the data to test to claim that the proportion of sensitive women is $\mathbf{0 . 0 2}$ greater than the proportion of sensitive men. Do not do this as a contingency table. (Use $\alpha=0.05$ for this test.)

| Gender | Men | Women |
| ---: | ---: | ---: |
| Sensitive | 20 | 42 |
| Insensitive | 180 | 238 |
| Total | 200 | 280 |

(8 points; 8 minutes)

1. A random sample of incoming freshmen was selected. Of the men, 22 chose sociology as a major and 191 did not. Of the women, 38 chose sociology and 219 did not. Use these results to prepare a $95 \%$ confidence interval for the difference in the proportions of all incoming men and women that will choose sociology as their major. Then use your results to answer this question:

Is it reasonable to claim that women and men choose Sociology in the same proportion?

YES NO Why?
(8 points - 10 minutes)

1. The data at the right represent two different acid treatments in an indistrial process. Use the information to construct a $98 \%$ confidence interval for $\mu_{1}-\mu_{2}$.
(Assume that $\sigma_{1}{ }^{2}=\sigma_{2}{ }^{2}$ )

| Treat. | Mean | Std. Nev. | N |
| ---: | ---: | ---: | :---: |
| Acid 1 | 11.620 | 1.185 | 10 |
| Acid 2 | 10.865 | 1.117 | 14 |


| Acid 1 | Acid 2 |
| ---: | ---: |
|  |  |
| 11.3 | 10.3 |
| 10.9 | 11.1 |
| 11.0 | 11.0 |
| 11.2 | 10.0 |
| 11.2 | 9.5 |
| 10.9 | 12.4 |
| 13.0 | 10.6 |
| 11.0 | 11.8 |
| 14.5 | 8.9 |
| 11.2 | 11.9 |
|  | 10.4 |
|  | 12.4 |
|  | 9.8 |
|  | 12.0 |

(8 points; 10 minutes)
6. Use the data below to construct a $90 \%$ confidence interval for the difference between the two population means from which the random samples were selected. Previous experiments have shown that the variability in Vitamin D levels is similar for both men and women.


Based on your results, is it reasonable to claim that men in general have more vitamin $D$ in their blood than women do? For credit, you must explain why?

Yes No Why?

## (7 points; 8 minutes)

11. A manufacturer of ceramic tiles compares two different curing temperatures to see which one makes the tiles stronger. Use the test data below to construct a $95 \%$ confidence interval for the difference between the population mean for 800 degrees and the population mean for 1200 degrees.
Experts advise you that the temperature difference is likely to cause a difference in the variability of the strength of the bricks.

(8 points - 10 minutes)
12. Use the information given here to test the claim that hot treatments require one more day for recovery on average than cold treatments. Use a significance level of 0.05 for this test.
(Assume that $\sigma_{1}{ }^{2}$ is not equal to $\sigma_{2}{ }^{2}$ )

|  | Recovery Time (Days) Treatment |  |
| :---: | :---: | :---: |
|  | Cold | Hot |
|  | 19 | 20 |
|  | 19 | 16 |
|  | 10 | 7 |
|  | 11 | 10 |
|  | 10 | 7 |
|  | 8 | 8 |
|  | 16 | 12 |
|  | 11 | 11 |
|  | 11 |  |
|  | 19 |  |
| Mean | 13.4 | 11.4 |
| Std. Dev. | 4.35 | 4.60 |
| n | 10 | 8 |

## (8 points: 12 minutres)

1. Do carpool lanes save commute time?

Transportation planners want to know whether carpool lanes save time for commuters. An experiment was carried out using 14 commuters who do not carpool and 11 commuters who do carpool. Use the summary of the survey results below to test the claim that carpool use does NOT save time, so the mean commute time for carpoolers is greater than or equal to the mean time for those who do not carpool. (Use $\alpha=0.01$ for the test and assume that variation is similar for both populations.)

| Time in Minutes |  |  |
| :---: | :---: | :---: |
|  | Regular Lanes | $\begin{aligned} & \text { pool } \\ & \text { ane } \end{aligned}$ |
| $\bar{x}=$ | 44.8 | 41.0 |
| $\mathrm{s}=$ | 15.1 | 13.6 |
| $\mathrm{n}=$ | 14 | 11 |

## (6 points - 8 minutes)

5. Use the information given here to test the hypothesis that the two samples ( $X$ and $Y$ ) come from "populations" for which $\sigma_{x}{ }^{2}$ is greater than $\sigma_{y}{ }^{2}$.
(Use $\alpha=0.025$ )
$\mathrm{H}_{0}$ : $\qquad$
$\mathrm{H}_{1}$ : $\qquad$

|  | Sample |  |
| :---: | :---: | :---: |
|  | X | Y |
|  | 103.3 | 43.3 |
|  | 105.0 | 17.4 |
|  | 101.5 | 21.2 |
|  | 114.2 | 58.7 |
|  | 102.4 | 37.7 |
|  | 103.1 | 40.1 |
|  | 94.2 |  |
|  | 114.7 |  |
| Mean | 104.8 | 36.4 |
| Std. Dev. | 6.79 | 15.15 |
| n | 8 | 6 |

(8 points - 8 minutes)
8. For each of the correlation coefficients given below, enter the letter of a graph from the following pages that best corresponds to the given correlation value.

There may be NONE or, perhaps, MORE THAN ONE GRAPH for any correlation.

| Correlation <br> Coefficient | Corresponding <br> Graph |
| :---: | :---: |
| $\rho=1.0$ |  |
| $\rho=-0.70$ |  |
| $\rho=0.90$ |  |
| $\rho=0.70$ |  |
| $\rho=-0.50$ |  |


| Correlation <br> Coefficient | Corresponding <br> Graph |
| :---: | :---: |
| $\rho=-0.90$ |  |
| $\rho=0.50$ |  |
| $\rho=0.00$ |  |
| $\rho=5.32$ |  |
| $\rho=-1.0$ |  |


(3 points, 5 minutes)
8. Assign one of the following correlation coefficients to each of the graphs to the right. (or state $r=$ none if no correlation coefficient seems appropriate for a graph)


(3 points, 5 minutes)
9. Assign one of the following correlation coefficients to each of the graphs to the right. (or state $r=$ none if no correlation coefficient seems appropriate for a graph)

(3 points, 5 minutes)
10. Assign one of the following correlation coefficients to each of the graphs to the right. (or state $r=$ none if no correlation coefficient seems appropriate for a graph)

(8 points)
3. Use the data provided below to test the claim that the population correlation ( $\rho$ ) between vehicle speed $(\mathrm{X})$ and miles per gallon $(\mathrm{Y})$ is less than zero. Assume the data are randomly selected. (Use $\alpha=0.01$ and do not use Table A.6)

Miles per
Observation Speed Gallon

| 1 | 28 | 32 |
| :--- | :--- | :--- |
| 2 | 35 | 27 |
| 3 | 50 | 28 |
| 4 | 75 | 25 |

(7 points; 8 minutes)
2. Market research concerning spending patterns found a sample correlation of 0.73 between $X=$ purchase price of house and $Y=$ purchase price of automobile for a sample of 10 families. Use these results to test the claim that the prices paid for houses and cars are positively correlated for the population of all families.
(Use a 0.10 significance level for this test.)

Claim: $\qquad$
$\mathrm{H}_{0}$ : $\qquad$
$\mathrm{H}_{1}$ : $\qquad$
(10 points - 15 minutes)
10. Use the data given below to answer questions (a) through (i).

| Test | $(\mathrm{X})$ <br> Fertilizer <br> Applied <br> Area <br> $(\mathrm{Kg} / \mathrm{Ha})$ | $(\mathrm{Y})$ <br> Harvested <br> Grain <br> $(\mathrm{Kg} / \mathrm{Ha})$ |
| :---: | :---: | :---: |
|  |  |  |
| 1 | 0 | 540 |
| 2 | 10 | 610 |
| 3 | 20 | 1018 |
| 4 | 40 | 1420 |
| 5 | 80 | 1548 |
| 6 | 120 | 1731 |

(a) Plot the data on the coordinate axes.
(b) Determine the equation of the regression line and write in in the space to the right:


Equation for line: $\qquad$
(c) If a farmer used 30 Kg of fertilizer per hectare, how much grain should be expected?
(d) What is the linear correlation between fertilizer applied and grain harvested? $\qquad$
(e) What is the value of the total variation in Y , the amounts of grain harvested? $\qquad$
(f) What fraction of the total variation in Y is explained by the regression line?
(g) What is the value of the explained variation in $Y$ ?
(14 points - 15 minutes)
4. Use the data shown for vehicle weight and fuel efficiency (miles per gallon of fuel) to answer the following questions.

| Data: | Fuel <br> Efficiency | Weight <br> (Ibs) |
| :---: | :---: | ---: |
| Vehicle | (mpg) |  |
| 1 | 41.7 | 1009 |
| 2 | 20.1 | 3275 |
| 3 | 24.0 | 3148 |
| 4 | 31.4 | 1269 |
| 5 | 32.9 | 1578 |
| 6 | 43.4 | 1206 |


(a) Plot the points on the graph
(b) What is the equation for the straight line that best predicts fuel efficiency ( y ) given vehicle weight ( x )?
(c) Plot the line on the graph.
(d) Based on you results, what is the predicted fuel efficiency for a vehicle that weighs 2500 lbs?
(e) What proportion of the total variation in $Y$ does your line explain?
(f) For the total variation in fuel efficiency (Y):

The expression is: $\qquad$ The value is: $\qquad$
(g) For the explained variation in fuel efficiency (Y):

The expression is: $\qquad$ The value is: $\qquad$
(h) For the unexplained variation in fuel efficiency ( $Y$ ):

The expression is: $\qquad$ The value is: $\qquad$
(i) For the Standard error of estimate:

The expression is: $\qquad$ The value is: $\qquad$
(8 points - 10 minutes)
4. A chain of shoe stores compares the sales for different shoe styles at their NEW California stores to the proportions during the last ten years at their New York stores. Use the data for 400 randomly selected sales in California to test the claim than California consumers buy the same styles of shoes in the same proportions as people in New York. (Use a Type l error rate of 0.05 for this test)

| Shoe Style | New <br> York <br> Rate | Observed <br> Counts in <br> Calif. |
| :---: | :---: | :---: |
| Flats | 0.15 | 50 |
| High heels | 0.25 | 60 |
| Athletic shoes | 0.35 | 140 |
| Sandals | 0.1 | 60 |
| Hiking Boots | 0.1 | 60 |
| Platform Shoes | 0.05 | 30 |

(10 points - 15 minutes)
3. The proportions of people in the U.S. that prefer 5 different kinds of entertainment are shown in the table below. A local survey of 500 people found 60 people who prefer movies, 200 who prefer to watch TV, 90 who like to listen to music, 30 who prefer dancing, and 120 that prefer to play sports. Test the claim that the true local proportions are the same as the national rates. (Use a 0.05 significance level for the test)

Claim: $\qquad$
Ho: $\qquad$
$H_{1}$ : $\qquad$

| Preferred <br> Entertainment | National <br> Rates | Local <br> Survey <br> Count |
| :--- | ---: | ---: |
| Watching <br> Movies | 0.15 | 60 |
| Watching <br> Television | 0.35 | 200 |
| Listening to <br> Music | 0.10 | 90 |
|  | 0.10 | 30 |
| Dancing | 0.30 | 120 |
| Playing <br> Sports | 500 |  |

7. A company that markets sodas does a survey of consumer preferences. Use the data to test whether the two age-groups (in general, not these specific individuals) have the same proportions that prefer each soda. (use $\alpha=0.025$ for the test)

(8 points - 10 minutes)
8. Use the data in the contingency table to test the claim that 2-year old boys and giris choose toys in the same proportions when placed in an observation room. (Use $\alpha=0.05$ for this test)

| Toy <br> chosen | Gender |  |  |
| :---: | ---: | ---: | ---: |
|  | Boys | Girls | Total |
| Ball | 40 | 20 | 60 |
| Doll | 5 | 25 | 30 |
| Bell | 5 | 5 | 10 |
| Total | 50 | 50 | 100 |

(10 points -20 minutes)
4. Use the data in the table to test the idea that the use of some "slang" terms is independent of age. The data represent a stratified random sample of 400 people from Los Angeles. (Use $\alpha=0.025$ for this test)

|  | Age Group |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: |
| Most used <br> Slang Term | 10 to 20 | 21 to 40 | 41 to 60 | $>60$ | Total |
| I'm like ... | 90 | 50 | 10 | 0 | 150 |
| totally | 10 | 40 | 40 | 10 | 100 |
| far out | 0 | 10 | 50 | 90 | 150 |
| Total | 100 | 100 | 100 | 100 | 400 |

6. Based on the data below, complete the Analysis of Variance Table by filling in the missing values. (Use $\alpha=0.01$ for the appropriate hypothesis test.)

| Years to Train for Professions |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Railroad <br> Engineer | Freighter <br> Captain | Airline <br> Pilot | Space Shuttle <br> Pilot |  |
| 2.0 | 4.0 | 3.0 | 6.0 |  |
| 2.8 | 1.5 | 5.5 | 2.8 |  |
| 3.2 | 2.0 | 4.0 | 5.0 |  |
|  | 1.0 | 2.9 | 5.0 |  |
|  | 3.4 |  | 3.6 |  |
|  | 0.8 |  | 4.0 |  |
| $\bar{x}=$ |  |  | 3.2 |  |
|  |  |  |  |  |
| $\mathrm{~s}=$ | 2.67 | 2.12 | 3.85 |  |
|  |  | 1.31 | 1.21 |  |


|  |  | Sum of | Mean <br> Source |
| :--- | :---: | :---: | :---: |
| d.f. | Squares | Square | F | p-value | Profession |
| :--- |
| Protween <br> (Broups) |
|  |
| Error <br> (Within <br> groups) |

(8 points : 10 minutes)
2. The Mayor of a city claims that the total fees paid by residents of similar sized cities are the same throughout the United States. Random samples of 20 residents in 26 cities of similar size are selected and the total fees they paid are determined (the data are on the following page). Use the data (as you may need to) to complete the analysis of variance table below. Then carry out a test of the Mayor's claim that average fees are the same for all $\mathbf{2 6}$ cities. (Use a significance level of 0.04 for this test.)

Analysis of Variance Table
$\mathrm{H}_{0}$ : $\qquad$
Analysis of Variance Table

|  | Degrees of <br> Source <br> Freedom | Sum of <br> Squares | Mean <br> Square | F |
| :--- | :---: | :---: | :---: | :---: | p-value |  |  |  |  |
| :--- | :--- | :--- | :--- |
| Cities |  |  |  |
|  |  |  |  |
| Error |  | 133329 |  |
| Total |  | 144886 |  |

$H_{1}$ : $\qquad$

Data on fees paid for 20 randomly selected residents in 26 cities in the U.S.

(3 points; 2 minutes)
11. Some people do not believe their driving is affected by drinking beer. A sample of 62 such sceptics takes part in an experiment, with the results listed below. Use the information given to complete the Analysis of Variance Table and test the idea that the mean number of errors is unaffected by the number of beers consumed.

Number of Errors Committed While Driving Test Course After Consuming the Indicated Number of Beers


Use alpha= 0.025 with the "Traditional Approach" for this test.

| SUMMARY |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: |
| Groups | Count | Sum | Average | Variance |
| 0 Beers | 8 | 37 | 4.6 | 5.13 |
| 1 Beers | 11 | 68 | 6.2 | 7.76 |
| 2 Beers | 7 | 88 | 12.6 | 45.62 |
| 3 Beers | 9 | 142 | 15.8 | 26.94 |
| 4 Beers | 6 | 131 | 21.8 | 151.77 |
| 5 Beers | 11 | 307 | 27.9 | 180.69 |
| 6 Beers | 10 | 374 | 37.4 | 188.04 |

Analysis of Variance Table

| Source of Variation | SS | $d f$ | $M S$ |
| :--- | :---: | :---: | :---: |
| Treatments (beers) |  |  |  |
| Error | 4860.924 |  |  |
| Total | 12995.5 |  |  |

(8 points : 10 minutes)

1. Use the data below to complete the Analysis of Variance Table and test the claim that all of the 1998 Chevy Nova cars have the same gas mileage today. (Use a 0.05 significance level for the test.)

|  | Test |  |  |  |  | Sample <br> Size | Mean |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | | Standard |
| ---: |
| Deviation |



| Analysis of Variance Table |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Deg. of |  |  |  |  |
| Sum of | Mean |  |  |  |
| Source | Freedom | Squares | Square |  |

Cars

## Error

Total

