

Statistics 300

Quiz #14

Name: \_\_\_\_\_

(8 points : 15 minutes)

1. Do carpool lanes save commute time? Use the results of the experiment below to test the claim that using the carpool lane causes the average commute time to be at least 5 minutes less per trip. For the experiment, 6 randomly selected routes from the suburbs to downtown were selected. For each route, the time required was tested using the regular lanes and using the carpool lane. The data are given below. Use a Type I error rate of 0.05 for the test.

Route	Time for Lane	
	Regular	Carpool
1	50.3	46.6
2	28.2	28.2
3	19.9	18.5
4	24.7	16.3
5	60.1	55.7
6	58.2	57.3
—		
$\bar{x}$ =	40.23	37.07
$s$ =	17.99	18.44
$n$ =	6	6

**Statistics 300**

**Quiz #14**

**Name:** \_\_\_\_\_

(8 points; 12 minutes)

2. The data are from an experiment to compare the effect of natural vitamins to synthetic vitamins. Six patients participated in the test. Each patient used the natural vitamins for 6 months and the synthetic vitamins for 6 months. The data are measurements of "energy level." Use the data to construct a 98% confidence interval for  $(\mu_1 - \mu_2)$ , the difference in mean energy level that would occur if all people participated in the experiment.

Patient	Vitamin Treatment	
	1 = Natural	2 = Synthetic
1	8	6
2	6	5
3	6	5
4	9	6
5	7	8
6	8	5
Mean	7.3	5.8
St. Dev.	1.21	1.17
n	6	6

**Statistics 300****Quiz #15**

Name: \_\_\_\_\_

(9 points:12 minutes)

- 1. Some people want to compare the proportion of high school boys that smoke cigarettes to the proportion of high school girls that smoke cigarettes. Use the data below to test the claim that the proportion of boys that smoke is 5% bigger than the proportion for girls. (Use the classical approach to hypothesis testing with a 0.10 significance level.)**

smoke	Girls	Boys
Yes	407	470
No	1451	1469

**Statistics 300****Quiz #15**

Name: \_\_\_\_\_

(9 points:12 minutes)

2. **Some people want to compare the proportion of high school boys that smoke cigarettes to the proportion of high school girls that smoke cigarettes. Use the data below to test the claim that the proportion of boys that smoke is the same as the proportion for girls. (Use the classical approach to hypothesis testing with a 0.10 significance level.)**

smoke	Girls	Boys
Yes	407	470
No	1451	1469

**Statistics 300****Quiz #15**

Name: \_\_\_\_\_

(9 points:12 minutes)

3. Some people want to compare the proportion of high school boys that are "overweight" to the proportion of high school girls that are "overweight". Use the data below to make an 80% confidence interval for the true difference between  $p_g$  (the proportion of all girls that are overweight) and  $p_b$  (the proportion of all boys that are overweight).

Overweight	Girls	Boys
Yes	418	486
No	1451	1469

(Blank page inserted here)

Statistics 300  
Quiz #16

Name: \_\_\_\_\_

(8 points : 12 minutes)

1. A random sample of 13 Zoologists has an average weight of 106 kg with a standard deviation of 22 kg. A random sample of 17 Physicists has an average weight of 100 kg and a standard deviation of 24 kg. Use these results to construct a 95% confidence interval for the difference between the mean weight of all zoologists and the mean weight of all physicists. (Assume that variation among weights is the same in both cases.) (You must include the algebraic expression for the test statistic as part of your answer.)

sample data		
	Zoologists	Physicists
n =	13	17
$\bar{X}$ =	106	100
s =	22	24

(8 points : 12 minutes)

2. A random sample of 16 Zoologists has an average weight of 106 kg with a standard deviation of 28 kg. A random sample of 10 Physicists has an average weight of 100 kg and a standard deviation of 20 kg. Use these results to test the claim that the mean weight of all zoologists is more than 2 kg greater than the mean weight of all physicists. (Assume that variation among the weights in each population may not be the same.) (You must include the algebraic expression for the test statistic as part of your answer.)

sample data		
	Zoologists	Physicists
n =	16	10
$\bar{X}$ =	106	100
s =	28	20

Statistics 300  
Quiz #16

Name: \_\_\_\_\_

(6 points : 10 minutes)

3. Some lawyers argue that police radar units are too variable to give reliable speed values. Police laboratories test a new radar unit that is claimed to have lower variability, and they compare its performance with an old unit. Use the test data to test the claim that the variability of the new radar unit is less than the variability of the old one. The readings from both units are normally distributed.

(Use a Type I error probability of 0.025.)

sample data		
	New Unit	Old Unit
n =	10	8
$\bar{x}$ =	68.4	68.3
s =	0.22	0.27

Claim: \_\_\_\_\_

H<sub>0</sub>: \_\_\_\_\_

H<sub>1</sub>: \_\_\_\_\_



Statistics 300  
Quiz #16

Name: \_\_\_\_\_

(8 points : 12 minutes)

4. You run a company that produces cans of mixed nuts labeled "400 grams". A requirement of the federal government is that the moisture content of the nuts (as a group) cannot be more than four percent (4 grams water per 100 grams of nuts). You have two different ways to measure the moisture content, called Method 1 and Method 2. Use the data below for 16 samples of nuts to make a 95% confidence interval for  $(\mu_1 - \mu_2)$ , the difference between the mean for Method 1 and the mean for Method 2. Assume that the two variances are the same. (You must include the algebraic expression for the CI in your answer.)

	Moisture (grams)	
Sample	Method 1	Method 2
1	21.4	19.8
2	23.6	23.2
3	12.6	12.4
4	22.9	22.1
5	16.0	14.6
6	19.2	17.9
7	17.9	17.6
8	16.1	15.3

---

$\bar{x}$ =	18.71	17.86
s =	3.80	3.73

Statistics 300  
Quiz #16

Name: \_\_\_\_\_

(8 points : 12 minutes)

5. You run a company that produces cans of mixed nuts labeled "400 grams". A requirement of the federal government is that the moisture content of the nuts (as a group) cannot be more than four percent (4 grams water per 100 grams of nuts). You have two different ways to measure the moisture content, called Method 1 and Method 2. Use the data below to test the claim that  $\mu_2$  is at least 0.5 grams more than  $\mu_1$ . (Let  $\alpha = 0.10$  and assume the variances for the methods are not the same. You must include the algebraic expression for the test statistic as part of your answer.)

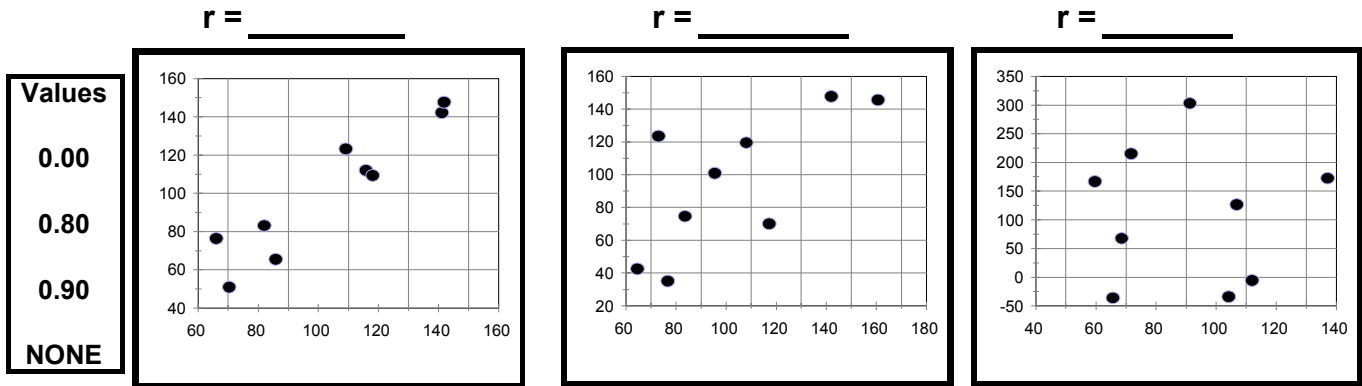
Moisture (grams)	
Method 1	Method 2
20.7	19.8
23.8	23.2
13.0	12.4
24.2	22.1
15.2	14.6
19.6	17.9
18.6	17.6
15.4	15.3
	18.6
	19.3

---

$\bar{x}$ =	18.81	18.08
s =	4.08	3.32

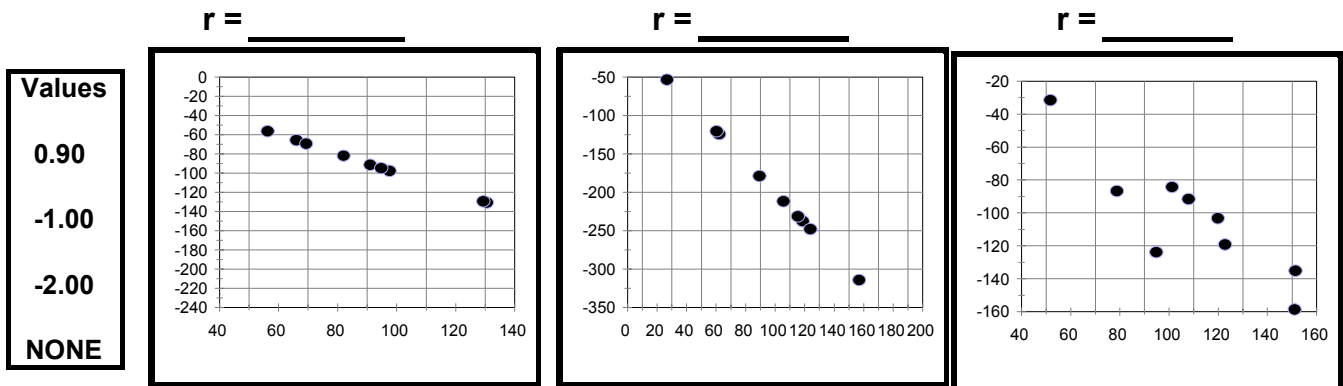
(3 points; 2 minutes)

1. Assign the three sample correlation coefficients to the three pictures. A correlation value may be used more than once or not at all. If a picture has no appropriate correlation available, write NONE [do not use the zero].



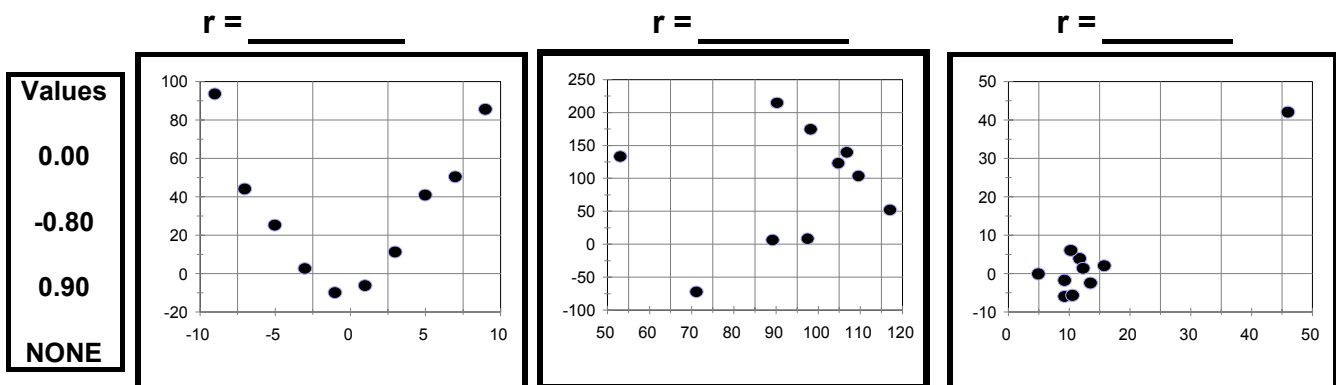
(3 points; 2 minutes)

2. Assign the three sample correlation coefficients to the three pictures. A correlation value may be used more than once or not at all. If a picture has no appropriate correlation available, write NONE [do not put zero].



(3 points; 2 minutes)

3. Assign the three sample correlation coefficients to the three pictures. A correlation value may be used more than once or not at all. If a picture has no appropriate correlation available, write NONE [do not use the zero].



(7 points; 8 minutes)

- 2. Market research concerning spending patterns found a sample correlation of 0.66 between  $X$ =purchase price of house and  $Y$ =purchase price of automobile for a sample of 6 families. Use these results to test the claim that the prices paid for houses and cars are positively correlated for the population of all families. (Use a 0.05 significance level for this test.)**

Claim: \_\_\_\_\_

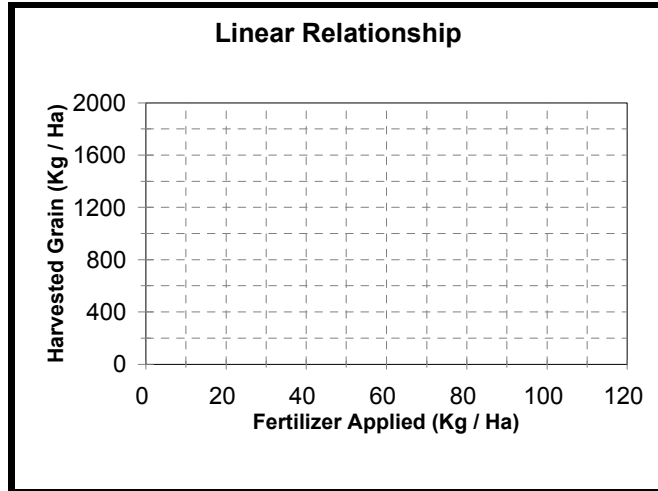
$H_0$ : \_\_\_\_\_

$H_1$ : \_\_\_\_\_

(15 points - 16 minutes)

3. Use the data given below to answer questions (a) through (i).

Test Area	(X) Fertilizer Applied (Kg / Ha)	(Y) Harvested Grain (Kg / Ha)
1	0	429
2	10	859
3	40	1572
4	80	1756
5	120	1256



- (a) Plot the data on the coordinate axes.
- (b) What is the equation of the least squares regression line for these data : \_\_\_\_\_
- (c) Plot the line on the graph.
- (d) If a farmer used 30 Kg of fertilizer per hectare, how much grain should be expected? \_\_\_\_\_
- (e) What is the linear correlation between fertilizer applied and grain harvested? \_\_\_\_\_
- (f) What is the expression for "total variation in Y" (amounts of grain harvested)? \_\_\_\_\_
- (g) What is the value of the total variation in Y, the amounts of grain harvested? \_\_\_\_\_
- (h) What fraction of the total variation in Y is explained by the regression line? \_\_\_\_\_
- (i) What is the expression for "explained variation in Y ?" \_\_\_\_\_
- (j) What is the value of the explained variation in Y? \_\_\_\_\_
- (k) What is the expression for "unexplained variation in Y ?" \_\_\_\_\_
- (l) What is the value of the unexplained variation in Y? \_\_\_\_\_
- (m) What is the expression for standard error of estimate,  $S_e$ ? \_\_\_\_\_
- (n) Determine the value of the standard error of estimate,  $S_e$ ? \_\_\_\_\_

(Blank page inserted here)

(8 points - 20 minutes : it's a big table)

1. Use the data in the contingency table to test the claim that customers at coffee vendors A, B, C, and D choose types of coffee beverages in the same proportions. (Use  $\alpha = 0.025$  for this test)

Coffee Choice	Vendor				Total
	A	B	C	D	
Plain	115	123	138	128	504
Latte	55	53	73	58	239
Mocha	80	74	39	64	257
Total	250	250	250	250	1000

Claim: \_\_\_\_\_

\_\_\_\_\_

$H_0$ : \_\_\_\_\_

\_\_\_\_\_

$H_1$ : \_\_\_\_\_

\_\_\_\_\_

(8 points - 10 minutes)

2. Use the data for a random sample of claims against auto insurance in Your City to test the claim that losses due to various causes occur in Your City in the same proportions that they occur in cities throughout the nation. (Use a Type I error rate of 0.05 for this test)

Type of Insurance Claim	Sample From Your City	National City Proportions
Theft	142	10%
Vandalism	78	9%
Fire	31	3%
Flood/Storm	10	2%
Collision	739	76%
Total	1000	100%

Claim: \_\_\_\_\_

H<sub>0</sub>: \_\_\_\_\_

H<sub>1</sub>: \_\_\_\_\_



**Statistics 300**  
**Quiz #19**

Name: \_\_\_\_\_

(8 points : 10 minutes)

1. Use the data below to complete the Analysis of Variance Table and test the claim that all of the 1998 Chevy Nova cars have the same gas mileage today. (Use a 0.05 significance level for the test.)

Car	Test				Sample Size	Mean	Standard Deviation
	1	2	3	4			
Car 1	20.33		20.63	17.00	3	19.32	2.015
Car 2	19.93	20.06	17.52		3	19.17	1.430
Car 3	17.53	18.50	17.10	20.87	4	18.50	1.685
Car 4	19.54	17.81	20.81	17.91	4	19.02	1.434
Car 5	20.39	20.33	18.56		3	19.76	1.040
Car 6	19.14	17.29	17.01	20.04	4	18.37	1.460
Car 7	19.77	20.60	19.08	19.96	4	19.85	0.626
Car 8	17.85	17.72	18.45		3	18.01	0.389
Car 9	19.10	17.09	17.45		3	17.88	1.072

Total N	Overall		Pooled
	Mean	St. Dev.	St. Dev.
31	18.88	1.331	1.335

Analysis of Variance Table				
Source	Deg. of Freedom	Sum of Squares	Mean Square	F
Cars				
Error				
Total				

**Statistics 300**  
**Quiz #19**

Name: \_\_\_\_\_

(8 points : 10 minutes)

2. Use the information below to test the claim that all of the 1998 Chevy Nova cars tested have the same gas mileage today.  
 (Use a 0.10 significance level for the test.)

Car	Test		
	1	2	3
Car 1	20.33	17.00	20.63
Car 2	19.93	20.06	17.52
Car 3	17.53	18.50	17.10
Car 4	19.54	17.81	20.81
Car 5	20.39	20.33	18.56
Car 6	19.14	17.29	17.01
Car 7	19.77	20.60	19.08
Car 8	17.85	17.72	18.45
Car 9	19.10	17.09	17.45

**Analysis of Variance:One Way**

**Summary**

<i>Groups</i>	<i>Count</i>	<i>Sum</i>	<i>Average</i>	<i>Variance</i>
Car 1	3	57.96	19.32	4.0593
Car 2	3	57.51	19.17	2.0461
Car 3	3	53.13	17.71	0.5143
Car 4	3	58.16	19.387	2.267633
Car 5	3	59.28	19.76	1.0809
Car 6	3	53.44	17.813	1.339633
Car 7	3	59.45	19.817	0.579233
Car 8	3	54.02	18.007	0.151633
Car 9	3	53.64	17.88	1.1487

**Analysis of Variance Table**

<i>Source of Variation</i>	<i>SS</i>	<i>df</i>	<i>MS</i>	<i>F</i>	<i>P-value</i>
Between Groups			2.3743		0.187788
Within Groups					
Total	45.369				