Statistics 300: Introduction to Probability and Statistics

Section 4-2

Probability

- Chapter 4
 - -Section 2: Fundamentals
 - -Section 3: Addition Rule
 - -Section 4: Multiplication Rule #1
 - -Section 5: Multiplication Rule #2
 - -Section 6: Simulating Probabilities
 - -Section 7: Counting

Fundamentals

- Vocabulary (Terms)
 - -Event
 - -Simple Event
 - -Sample Space

Example Procedures

- Roll a die; record value
- Roll 2 dice; record sum
- Survey 50 people; count "no's"
- Select 200 people at random; take heights; record average

Event

- The result of a procedure
- Examples:
 - -Value of die is 4
 - -Sum of 2 dice is 10
 - -The average height of 200 people is 64.83 inches

Events: Simple or Compound

- Simple
 - -Can only occur in one way
- Compound
 - -Can occur in multiple ways

Events: Simple or Compound

- Examples:
 - -Value of die is 4 : simple
 - -Sum of 2 dice is 10 : compound
 - -The avg. height of 200 people is 64.83 inches : compound

Sample Space

- The collection of all possible simple events
- See EXCEL example for rolling two dice

Notation for Probabilities

- "P" denotes "the probability of"
- A, B, C, etc. denote specific events
- So we read "P(A)" as "the probability of A"

Probability Notation (try some on overhead)

What is a Probability?

- No definition is universally accepted
- Mine: A relative frequency that has not happened yet
- Sophisticated math definitions
- Degree of belief

Determining Probabilities

- Experience
 - -Rule 1: Observe the relative frequency over many trials
- Logic
 - -Rule 2: Deduce the relative frequency based on principles

Experience: Rule 1

- Relative Frequency Approximation of Probability
- Conduct a procedure many times; observe the relative frequency
- **P**(**A**) = (count **A** / total count)

Try this: If I drop my right shoe from shoulder height, what is the probability that it will land upright?

Logic: Rule 2

- Classical Approach to Probability
- Determine the number of ways that event "A" can occur
- Determine the number of all possible outcomes
- **P**(**A**) = (ways for **A**)/(all ways)

Try this: What is the probability that I will get a 6 when I roll a die?

Complementary Events

- The complement of event "A" consists of all possible outcomes for which "A" does not occur
- Denoted "A" with a line over the top
- P(A) is "Probability of not A"
 - $-\mathbf{A} = \mathbf{a}$ woman is selected, then $-\overline{\mathbf{A}} = \mathbf{a}$ woman is not selected
 - -A = a woman is not selected