Statistics 300:
Introduction to Probability and Statistics
Summer 2016 Day Class
Cosumnes College

Instructor: L.C. Larsen

Instructions

Time: 2 hours and 10 minutes
Date: 28-Jul-16

Materials: Open book, notes, homework, quiz sets, example problems, study guides, etc.

Instruments: Calculator/tablet/Laptop of student's choice

No phone calls or consultants except for questiods addressed to the instructor.

Answers to confidence interval problems must include the expression (the formula) in symbolic form and the expression with all of the values inserted in the proper places. Then, the final answer can be calculated by any method or device.

Unless a p-value is given in the problem, each hypothesis test problem must include all four parts of the traditional approach to hypothesis tests, including the expression (the formula) for the test statistic in symbolic form and the expression with the values in the right places. The result can then be calculated by whatever method you like (TI-83, laptop computer, etc.).

If a p-value is given in the problem, the conclusion must be based on a proper comparison of the $p$-value to the significance level.

If more space is needed for a problem, continue your work on the back of the page.
(9 points; 9 minutes)

1. Use the data below to make a $98 \%$ confidence interval for the difference between the proportion of people in New York that say they "mainly use public transit" and the proportion of people in Chicago that say they "mainly use public transit".

| City | I mainly use public transit |  |
| :---: | :---: | :---: |
|  | Yes | No |
| New York | 730 | 270 |
| Los Angeles | 230 | 770 |
| Chicago | 675 | 325 |

Based on your confidence interval, is it reasonable to claim that "The proportion of New York residents that mainly use public transit is the same as the proportion of Chicago residents that mainly use public transit" ?

Yes No Why?
(8 points; 8 minutes)
2. Use the data shown in the table to test the claim that the time (hours) needed for paint to dry is negatively correlated with temperature.
(Let $\alpha=0.025$ for this test.)

| Temperature <br> ${ }^{\circ} \mathrm{C}$ | Hours <br> Needed <br> to Dry <br> Paint |
| :---: | :---: |
|  |  |
| 5 | 41 |
| 10 | 35 |
| 15 | 28 |
| 20 | 31 |
| 25 | 27 |

$\mathrm{H}_{0}$ : $\qquad$
$\mathrm{H}_{1}$ : $\qquad$
(10 points; 10 minutes)
3. Cancer patients were treated with two anti-cancer drugs: Drug A and Drug B. Use the results shown in the table to test the hypothesis that the two drugs are equally effective in curing cancer, so the percent of patients cured is the same.
(Use a $10 \%$ significance level for this test.)

$\mathrm{H}_{0}: \ldots \quad$| Response of Cancer Patients |  |  |
| :---: | :---: | :---: |
|  |  | Drug A |
| Cured | 291 | Drug B |
| Not Cured | 119 | 219 |
| Total | 410 | 226 |

(9 points; 9 minutes)
4. Pollutants in the water from the City water treatment plant are measured in samples taken during the Spring (May ) and Summer (August). Use the statistics given here to make a 95\% confidence interval for the difference between the the population mean for pollutant measurments in May and the population mean for pollutant measurementsin August. The variation in May measurements is similar to the variation in August measurements.

| Amount of Pollutants |  |  |
| ---: | :---: | :---: |
| Sample <br> Statistics | Month |  |
| $\mathrm{N}=$ | 18 | 14 |
| Average $=$ | 78 | 84 |
| Std. Deviation $=$ | 11 | 10 |

Based on your interval is it reasonable to say that the average amount of pollutant in the water in May is $\mathbf{7 4}$ and the average amount of pollutant in the water in August is $\mathbf{8 8}$ ?

Yes
Why?
No
(13 points; 13 minutes)
5. Plot the appropriate test scores as points (score $A$ as $X$, and score $C$ as $Y$ ) on the graph axes.

Each row in the dataset is for a different person. Then answer parts $\mathbf{b}, \mathrm{c}, \mathrm{d}, \mathrm{e}, \mathrm{f}$, and g .

| Person | Exam Scores |  |  |
| :---: | :---: | :---: | :---: |
|  | A | B | C |
| 1 | 90 | 84 | 100 |
| 2 | 78 | 70 | 78 |
| 3 | 73 | 82 | 62 |
| 4 | 59 | 52 | 48 |
| 5 | 38 | 35 | 40 |
| 6 | 50 | 42 | 65 |
| 7 | 98 | 92 | 98 |

(a) Plot the points on the graph.

(b) Use your calculator to determine the equation of the line that best predicts the Test C score based on a known score for Test A.

Equation of your line : $\qquad$
(c) Plot your line on the graph.
(d) What is the linear correlation between the scores for Test A and Test C?
(e) Provide the symbolic expressions for Total, Explained, and Unexplained variation in "Y".

(f) Provide the values for Total, Explained, and Unexplained variation in " Y " for the graphed data.

(g) Provide the symbolic expression and the value for the Standard Error of Estimate.

[^0]Value
$\qquad$
(9 points; 10 minutes)
6. Random samples of $\mathbf{6 0 0}$ people from three age groups were asked what size of car they drove -- Large, Medium, or Small. Use the data below to test the claim that all people in the three age-groups drive Large, Medium, and Small cars in the same proportions. (Use a 0.025 significance level for this test.)

| Age Group | Size of Car |  |  | Row <br> Total |
| :---: | :---: | :---: | :---: | :---: |
|  | Large | Medium | Small |  |
| $<30$ | 142 | 206 | 252 | 600 |
| 30 to 40 | 150 | 220 | 230 | 600 |
| $>40$ | 218 | 180 | 202 | 600 |
| Col. Total | 510 | 606 | 684 | 1800 |

Claim:
$\mathrm{H}_{0}$ :
$\mathrm{H}_{1}$ :
(9 points; 10 minutes)
7. A City studied the effects of visible police presence on average driving speed. Use the data below to test the claim that the average driving speed is more than five miles per hour faster when police are not visibly present compared to when police are visibly present. Variability in driving speeds increases when police are not visibly present. (Treat the data as "simple random samples", and let $\alpha=5 \%$.)

| Hourly Values for Driving Speed <br> with Police "Visible" and "Not Visible" |  |  |
| :---: | :---: | :---: |
| Sample <br> Statistic | Visible | Not |
| $n=$ | 31 | 21 |
| mean $=$ | 66.4 mph | 72.8 mph |
| st. dev. $=$ | 3.4 mph | 5.2 mph |

## Claim:

$\qquad$
$\mathrm{H}_{0}$ : $\qquad$
$\mathrm{H}_{1}$ : $\qquad$
$\qquad$
(6 points; 6 minutes)
8. Connect each picture with one of the candidate correlation ( $\mathbf{r}$ ) values by writing the appropriate candidate " $r$ " value in the space at the top of each graph.

| Candidate values of "r", the sample correlation coefficient. |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.00 | -0.50 | -0.90 | -1.00 | 0.50 | 0.90 | 1.00 | 2.00 |



Name:
(9 points; 7 minutes)
10. The Analysis of Variance table below is based on the 304 data values on the next page. Complete the AOV table and test the claim that types of glass made by ten different makers of windows lose the same average amount of energy. Use a $\mathbf{2 \%}$ significance level for the test based on the p-value approach to hypothesis testing.

AOV Table

|  | Sum of <br> Source | Squares | df | Mean <br> Square | F |
| :--- | :---: | :---: | :---: | :---: | :---: | p-value | Sroducers | 544 |  |  | 0.099718 |
| :--- | :---: | :--- | :--- | :--- |

Error

Total 11288

$$
\mathrm{H}_{0}:
$$

$H_{1}$ :

Energy losses through windows made from 10 different types of glass
Type_1 Type_2 Type_3 Type_4 Type_5 Type_6 Type_7 Type_8 Type_9 Type_10

| 96 | 92 | 107 | 99 | 102 | 95 | 103 | 102 | 93 | 98 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 88 | 97 | 102 | 101 | 92 | 109 | 95 | 98 | 106 | 107 |
| 107 | 101 | 110 | 99 | 109 | 94 | 93 | 105 | 110 | 106 |
| 100 | 106 | 103 | 108 | 93 | 90 | 94 | 94 | 102 | 90 |
| 96 | 106 | 108 | 104 | 107 | 110 | 95 | 107 | 99 | 95 |
| 90 | 97 | 97 | 102 | 110 | 105 | 98 | 106 | 99 | 91 |
| 91 | 97 | 101 | 98 | 94 | 98 | 90 | 100 | 104 | 98 |
| 93 | 93 | 95 | 102 | 103 | 94 | 105 | 98 | 106 | 93 |
| 91 | 104 | 99 | 105 | 100 | 99 | 98 | 92 | 108 | 101 |
| 97 | 106 | 105 | 92 | 97 | 108 | 97 | 101 | 102 | 109 |
| 98 | 93 | 99 | 90 | 90 | 92 | 105 | 90 | 104 | 104 |
| 90 | 98 | 105 | 99 | 90 | 95 | 110 | 100 | 91 | 99 |
| 95 | 99 | 90 | 99 | 107 | 98 | 100 | 104 | 90 | 93 |
| 96 | 93 | 110 | 109 | 102 | 109 | 108 | 105 | 99 | 92 |
| 99 | 96 | 102 | 91 | 105 | 97 | 96 | 93 | 97 | 93 |
| 106 | 101 | 92 | 96 | 100 | 92 | 90 | 105 | 99 | 99 |
| 90 | 104 | 93 | 100 | 98 | 93 | 97 | 95 | 90 | 95 |
| 89 | 92 | 110 | 90 | 103 | 92 | 106 | 103 | 110 | 99 |
| 99 | 98 | 92 | 98 | 109 | 108 | 101 | 102 | 96 | 103 |
| 89 | 98 | 91 | 96 | 94 | 93 | 108 | 95 | 93 | 92 |
| 103 | 106 | 95 | 108 | 103 | 96 | 110 | 103 | 90 | 90 |
| 100 | 110 | 108 | 105 | 93 | 102 | 96 | 106 | 97 | 93 |
| 103 | 109 | 90 | 91 | 108 | 101 | 95 | 93 | 108 | 92 |
| 94 | 95 | 99 | 93 |  | 109 | 98 | 91 | 110 | 105 |
| 101 | 94 | 95 | 96 |  | 100 | 109 | 102 | 106 | 96 |
| 102 | 105 | 102 | 96 |  | 93 | 96 | 91 | 108 |  |
| 94 | 101 | 110 | 108 |  | 104 | 104 | 103 | 110 |  |
| 93 | 107 | 93 | 108 |  | 95 | 95 | 108 | 94 |  |
| 95 | 109 | 95 | 110 |  | 97 | 96 | 99 | 102 |  |
| 94 | 104 | 108 | 105 |  | 104 | 99 | 105 | 92 |  |
| 105 | 103 | 96 |  |  |  | 110 | 101 |  |  |
| 101 | 99 | 98 |  |  |  | 107 | 91 |  |  |
|  | 90 |  |  |  |  | 105 |  |  |  |
|  | 104 |  |  |  |  | 108 |  |  |  |
|  | 100 |  |  |  |  | 101 |  |  |  |
| 32 | 35 | 32 | 30 | 23 | 30 | 35 | 32 | 30 | 25 |
| 96.4 | 100.2 | 100.0 | 99.9 | 100.4 | 99.1 | 100.5 | 99.6 | 100.5 | 97.3 |
| 5.4 | 5.6 | 6.6 | 6.1 | 6.5 | 6.3 | 6.0 | 5.5 | 6.8 | 5.7 |

$\qquad$
(8 points; 8 minutes)
11. A local newspaper surveyed 900 likely voters and asked each person how likely they were to vote for the candidate currently representing their district. Use the data below to test the claim that the proportions today are the same as the proportions from another taken before the previous election for district representative. Let $\alpha=0.05$.

| Results of current <br> election survey |  | Last <br> Survey |
| :---: | :---: | :---: |
| Very <br> Likely | 284 | $32 \%$ |
| Somewhat <br> Likely | 308 | $27 \%$ |
| Equally <br> Likely and <br> Unlikely | 100 | $12 \%$ |
| Somewhat <br> Unlikely | 120 | $18 \%$ |
| Very <br> Unlikely | 88 | $11 \%$ |
| Total |  | 900 |

$\mathrm{H}_{0}$ : $\qquad$
$\qquad$
$\mathrm{H}_{1}$ : $\qquad$


[^0]:    Symbolic Expression

