Statistics 300 : Fall 2017 (Saturday class)
Instructor : L. C. Larsen

Name (print):

Los Rios ID\#:

Signature:

## Exam : Unit 1

Time allowed : 2 hours and 10 minutes

Resources allowed:
$==>$ Textbook (Author: Nividi and Monk)
$==>\quad$ Notes/helps written by the student
$==>\quad$ Quiz and exam solutions written by instructor
$==>$ Quiz and exam solutions written by the student
$==>\quad$ Calculator/laptop/tablet of choice (no outside contacts)
$==>\quad$ Instructor at 916-346-6324

Resources not allowed:
$==>\quad$ Consultants other than the instructor
$==>\quad$ No phones, unless used as a calculator only

1. Use the data for the sample represented in the following table to answer parts (a) through (e).
(1 point, 1 minute)
(a) What is the probability that a randomly selected person will have "High School" as their highest level of schooling?

| Highest Level <br> of Schooling | Income Quartile |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: |
|  | First | Second | Third | Fourth | Total |
| Graduate | 87 | 121 | 437 | 591 | 1236 |
| College | 191 | 285 | 446 | 580 | 1502 |
| High School | 274 | 203 | 328 | 267 | 1072 |
| Elementary | 239 | 254 | 151 | 139 | 783 |
| None | 772 | 389 | 131 | 62 | 1354 |
| Total | 1563 | 1252 | 1493 | 1639 | 5947 |

(3 points, 3 minutes)
(b) What is the probability that a person randomly selected from this sample will have income in the "Second Quartile" given that the person has "Graduate" level schooling?
(3 points, 3 minutes)
(c) What is the probability that a person randomly selected from this sample will have "None" education or "Graduate" education?
(3 points, 3 minutes)
(d) What is the probability that a person randomly selected from this sample will have income in the "First Quartile" or "High School" as their highest education level?
(3 points, 3 minutes)
(e) What is the probability that a person randomly selected from this sample will not be a person in the "First Quartile" for income who also has "Graduate" level schooling?
(4 points and 3 points; 8 minutes)
2. (a) Use the information provided to determine the lower number and the higher number between which you expect to find almost all (~99.7\%) of the data.

(b) Would a value of $\mathbf{2 5 0}$ or more from this distribution be considered "unusual" ? [must show why]

Circle: YES of NO
(10 points; 8 minutes)
Complete the columns in the "Frequency Distribution" table using the data values given below, and answer the two questions beoow the table.

Frequency Distribution

| Class  <br> Limits  <br> Lower Upper | Tally | Frequency | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative <br> Frequency |  |
| :---: | :---: | :--- | :--- | :--- | :--- | :--- |
| 6.5 | 7.0 |  |  |  |  |  |
| $>7.0$ | 7.5 |  |  |  |  |  |
| 7.5 | 8.0 |  |  |  |  |  |



| Data: | 7.7 | 7.3 | 7.4 | 8.0 | 7.7 |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | 7.7 | 6.5 | 7.6 | 7.8 | 7.5 |



What is the frequency for Class \#3 ?
What is the lower limit for Class \#2?
(4 points; 6 minutes)
4. For the study described below, select the appropriate statistical terms from the list provided and write them in the blanks, choose the term that is best connected to the underlined text.

| Terms: | randomization | placebo |
| :--- | :--- | :--- |
|  | replication | block |
|  | confounding | experimental unit |
|  | blinding | treatment |

a.

Engineers test the strength of concrete for use by homeowners. Forty homeowners take part in a the study. Twenty homeowners are randomly assigned to use "concrete mix \#1" and the other twenty homeowners use "concrete mix \#2", which has extra ingredients. Neither the homeowners nor the engineers know who is using which mix. Each homeowner mixes the concrete and pours a square slab 10 feet by 10 feet and 4 inches thick. No effort is made to control factors like daily temperature that could affect the strength of the concrete. The experiment shows that the extra ingredients improve the concrete strength by a large amount.
b.

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## (4 points and 5 points; 10 minutes)

5. Use the dataset at the bottom of this page to answer parts (a), (b) and (c).

There are 130 values in the dataset, in rows of 10, sorted from the smallest at the top to the largest at the bottom.
(a) What percentile is represented by the value 2136 ?
(c) Using the number line below, make a Boxplot to represent the distribution of the dataset. Use a simple " 5 -number summary" to prepare this boxplot.


| 100 | 107 | 144 | 149 | 170 | 193 | 200 | 226 | 263 | 294 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 322 | 340 | 344 | 363 | 372 | 385 | 402 | 440 | 475 | 514 |
| 523 | 545 | 584 | 599 | 627 | 657 | 669 | 697 | 715 | 740 |
| 752 | 770 | 778 | 830 | 863 | 963 | 988 | 1015 | 1042 | 1070 |
| 1073 | 1087 | 1169 | 1223 | 1278 | 1335 | 1365 | 1430 | 1484 | 1521 |
| 1551 | 1564 | 1603 | 1613 | 1657 | 1727 | 1791 | 1798 | 1877 | 1904 |
| 1934 | 1948 | 1948 | 1954 | 1962 | 1966 | 1970 | 1980 | 1985 | 1989 |
| 1994 | 2004 | 2012 | 2020 | 2029 | 2032 | 2041 | 2047 | 2057 | 2063 |
| 2063 | 2068 | 2070 | 2080 | 2090 | 2098 | 2102 | 2112 | 2121 | 2125 |
| 2128 | 2131 | 2136 | 2137 | 2140 | 2142 | 2146 | 2155 | 2161 | 2161 |
| 2165 | 2174 | 2183 | 2193 | 2195 | 2204 | 2210 | 2216 | 2219 | 2222 |
| 2228 | 2229 | 2229 | 2231 | 2237 | 2243 | 2251 | 2255 | 2264 | 2266 |
| 2272 | 2279 | 2286 | 2289 | 2293 | 2301 | 2310 | 2315 | 2318 | 2324 |

(4 points and 2 points; 5 minutes)
6. You have four M\&Ms, one green, one blue, one red, and one yellow. Two of the M\&Ms will be picked, one at a time, without replacement. List the sample space for this procedure. Example: RY, meaning the first is "red" and the second is "yellow".

If the two M\&Ms are picked in a random order and without replacement, what is the probability that the red M\&M will be picked but the blue M\&M will not be picked?
(3 points; 3 minutes)
7. A lucky person is picked at random as the Grand Prize winner in a lottery. The winner will pick one of four cars, one of five houses, and one of six TVs. How many different ways can the winner pick a combination of one car, one house, and one TV?
(3 points; 3 minutes)
8. A person has eight siblings (brothers and sisters). The person also has a picture of each sibling. If the pictures are to be hung at equal height along one wall of the living room, how many different ways can the pictures be arranged?
(5 points; 6 minutes)
9. A creator of carnival rides wants to use the $10^{\text {th }}$ and $90^{\text {th }}$ percentiles of the heights all 10 -year-old children to help in designing a new "roller coaster" ride. A random sample of 450 10-year-old children is selected and their heights are measured. The $10^{\text {th }}$ and $90^{\text {th }}$ percentiles of these heights were 48 inches and 56 inches.

Use the information in the "story" to answer the following:
(a) What is the population of interest to the creator of carnival rides?
(b) The creator of carnival rides wanted to know the value(s) of what population parameter(s)?
$\qquad$
$\qquad$
(c) The creator of carnival rides determined the value(s) of what statistic(s)?
(d) What were the value(s) that the creator of carnival rides determined for the statistic(s) in part (c)?
(e) Was a sample or a census used, and how did you decide your answer?
(14 points; 8 minutes)
10. Use the data below to determine the value of each statistic. Write an expression for each statistic or describe how it is calculated in principle (do NOT describe how to use the calculator to determine the result).


## (3 points; 3 minutes)

13. Last year, a small High School had 60 students, of which 39 were girls (G) and 21 were boys ( $B$ ). If 5 of the 60 students are selected at random (without replacement), what is the probability that the exact order will be $\{\mathrm{G}, \mathrm{G}, \mathrm{B}, \mathrm{B}, \mathrm{G}\}$ ?
(Show your work.)
(3 points; 3 minutes)
14. A final exam in statistics must have 10 out of $\mathbf{2 6}$ possible problems. If the professor decides to choose the $\mathbf{1 0}$ problems at random and then arrange them in a random order, how many different ways could the test turn out?
(3 points; 3 minutes)
15. A statistics exam will have 2 different versions so students will be discouraged from trying to cheat. The class has 36 students and will be divided into two groups of 18 each. Group 1 will get test \#1 and group 2 will get test \#2. How many ways could the professor divide the class into two groups 18 ?
(3 points; 3 minutes)
16. From a very large population (millions of values), what is the probability that two random values (treat them as independent) will both be between the $30^{\text {th }}$ and the $62^{\text {nd }}$ percentiles ( $\mathrm{P}_{30}$ and $\mathrm{P}_{60}$ ).
(3 points; 3 minutes)
17. Circle the best answer for each situation.

Official surveyers call 4,000 people who are randomly selected from those that used Medical health services in the last 10 years. Of the $\mathbf{4 0 0 0}$ people, $\mathbf{2 2 \%}$ agree to take the the survey, and these are asked if they know their estate must repay the costs when they die.

| Simple Random | Systemmatic |
| :--- | :--- |
| Stratified Random | Cluster |
| Convenience | Census |

A government program auditor reviews Medical case files. Files for every Medical provider (hospital, doctor, pharmacy, etc.) will be reviewed. For each provider, the auditor will examine every $200^{\text {th }}$ file.

| Simple Random | Systemmatic |
| :--- | :--- |
| Stratified Random | Cluster |
| Convenience | Census |

The DMV provides a list of all registered vehices to a research group for study. The researchers attach a random value between zero and one to each vehicle's record. The 200 records with the smallest random values are selected as the sample to study.

| Simple Random | Systemmatic |
| :--- | :--- |
| Stratified Random | Cluster |
| Convenience | Census |

18. Circle the correct choice in each box in relation to the underlined text.

|  | Are the data ...? | Are the data ...? |
| :---: | :---: | :---: |
| a. A grocery store sells eggs that are small, medium, large, and extra large. On September 11, 2001, the store sold 127 pounds of eggs. | Qualitative <br> Quantitative and Discrete Quantitative and continuous | Nominal Interval <br> Ordinal Ratio |
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| Qualitative <br> Quantitative and Discrete <br> Quantitative and continuous | Nominal Interval |
| :--- | :--- | :--- |

