

If a parabola is lined up with either the x -axis or y -axis, the equation will look like one of these:

$(x - h)^2 = 4p(y - k)$ This parabola has vertex (h, k) and opens up. The focus is p units above the vertex and the directrix is a horizontal line p units below the vertex.

$(x - h)^2 = -4p(y - k)$ This parabola has vertex (h, k) and opens down. The focus is p units below the vertex, and the directrix is a horizontal line p units above the vertex.

$(y - k)^2 = 4p(x - h)$ This parabola has vertex (h, k) and opens to the right. The focus is p units to the right of the vertex, and the directrix is a vertical line p units to the left of the vertex.

$(y - k)^2 = -4p(x - h)$ This parabola has vertex (h, k) and opens to the left. The focus is p units to the left of the vertex, and the directrix is a vertical line p units to the right of the vertex.

An ellipse centered at (h, k) , with long axis horizontal has equation

$$\frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1, \text{ where } a > b.$$

An ellipse centered at (h, k) , with long axis vertical has equation

$$\frac{(y - k)^2}{a^2} + \frac{(x - h)^2}{b^2} = 1, \text{ again where } a > b.$$

For an ellipse, $a^2 = b^2 + c^2$

A hyperbola centered at (h, k) , opening left and right has equation

$$\frac{(x - h)^2}{a^2} - \frac{(y - k)^2}{b^2} = 1, \text{ with no condition on } a \text{ and } b.$$

A hyperbola centered at (h, k) , opening up and down has equation

$$\frac{(y - k)^2}{a^2} - \frac{(x - h)^2}{b^2} = 1, \text{ again with no condition on } a \text{ and } b.$$

The a always matches up with the positive term, and the b with the negative term.

For a hyperbola, $c^2 = a^2 + b^2$

A circle centered at (h, k) , with radius r has equation

$$(x - h)^2 + (y - k)^2 = r^2$$